

Idade = variável x

Variável y

	19-20	21-22	23-24	25-26	27-28	29-30	31-32	33-34	35-36	37-38	39-40	41-42	43-44	f	d	fd	fd ²
0-4											1			1	-13	-13	169
5-9						1					2			2	-12	-24	288
10-14						2					3			3	-11	-33	363
15-19					1	1					3			3	-10	-30	300
20-24			1		1	1					6			6	-9	-54	486
25-29			2		1	1					3			3	-8	-24	192
30-34		1	1		1	2					13			13	-7	-91	637
35-39		2	1		1	1					6			6	-6	-36	216
40-44		1	1		1	1					9			9	-5	-45	225
45-49		1	1		1	1					7			7	-4	-28	112
50-54		1	1		1	1					16			16	-3	-48	144
55-59		1	1		1	1					14			14	-2	-28	56
60-64		1	1		1	1					22			22	-1	-22	32
65-69		1	1		1	1					55			55	0	-476	
70-74		1	1		1	1					51			51	+1	+51	51
75-79		1	1		1	1					43			43	+2	+146	292
80-84		1	1		1	1					68			68	+3	204	612
85-89		1	1		1	1					53			53	+1	212	944
90-94		1	1		1	1					42			42	+5	210	1050
95-99		1	1		1	1					24			24	+6	126	766
100-104		1	1		1	1					2			2	+7	14	98
Σ	7	82	36	20	36	38	46	2	3	0	1	0	1	963			6717
Σd	-9	-2	-4	0	+1	+2	+3	+4	+5	+6	+7	+8	+9	441			-150
Σd ²	81	24	16	0	1	4	9	16	25	36	49	64	81	1510			

$\Sigma(x-y) = -650$

$C = \frac{484}{470} \times 5 = 1,036 \times 5 = 5,180$

$M = 67,5 + 5,180 = 72,680$

$\sigma = 5 \sqrt{\frac{6917}{470} - 1,036^2} = 5 \times 3,693 = 18,465$

$C.V. = \frac{18,465}{72,680} \times 100 = 25,4$

Variável x

$C = \frac{150}{470} \times 2 = 0,319 \times 2 = 0,638$

$M = 26 + 0,638 = 26,638$

$\sigma = 2 \sqrt{\frac{1510}{470} - 0,319^2} = 2 \times 1,763 = 3,526$

$C.V. = \frac{3,526}{26,638} \times 100 = 13,2$

Coefficiente de correlação

$r = \frac{-650}{470} - (1,036 \times 0,319) \times 10 = \frac{-18,465 \times 3,526}{18,465 \times 3,526}$

$= \frac{-(1,382 - 0,330484)}{65,10540} \times 10 =$

$= \frac{-1,712484}{65,10540} \times 10 =$

$= -0,260 \times 10 = -2,60$

$\sigma = \frac{1 - 0,260^2}{\sqrt{470}} =$

$= \frac{1 - 0,067600}{31,69} =$

$= \frac{0,932400}{21,69} = \pm 0,043$

Idade = variável x

Variável y

$$c = \frac{56}{241} \times 2 = 0,232 \times 2 = 0,464$$

$$M = 24,5 + 0,464 \times 28,660$$

$$\sigma = 5 \sqrt{\frac{1430}{241} - 0,232^2} = 5 \times 2,21 = 11,05$$

$$O.V. = \frac{12,120}{28,660} \times 100 = 42,3$$

Variável x

$$c = \frac{103}{241} \times 2 = 0,427 \times 2 = 0,854$$

$$M = 27 + 0,854 = 27,854$$

$$\sigma = 2 \sqrt{\frac{1497}{241} - 0,427^2} = 2 \times 2,404 = 4,808$$

$$O.V. = \frac{4,808}{27,854} \times 100 = 17,2$$

Coefficiente de correlação

$$r = \frac{-258}{241} - (0,232 \times 0,427) \times 10 =$$

$$= \frac{-(1,046 - 0,099064)}{0,8,2 + 2,760} \times 10 =$$

$$= \frac{-1,175064}{0,8,2 + 2,760} \times 10 =$$

$$= -0,020 \times 10 = -0,200$$

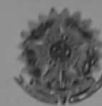
$$\sigma_y = \frac{1,0200}{\sqrt{241}}$$

$$= \frac{1 - 0,040000}{15,32} =$$

$$= \frac{0,960000}{15,52} = \pm 0,061$$

	20-21	22-23	24-25	26-27	28-29	30-31	32-33	34-35	36-37	38-39	40-41	f	d	fd	fd²
0-4		1 ₁₀	1 ₅	1 ₅		1 ₁₀		3 ₆₀	1 ₂₅			8	-5	-40	200
5-9			3 ₁₂	3 ₄	2 ₈	1 ₈	1 ₁₂	3 ₁₈				13	-4	-53	208
10-14	1 ₉		2 ₆	1 ₃	2 ₆		1 ₉	1 ₁₂	3 ₁₆			8	-3	-24	73
15-19	1 ₆	1 ₁₀	5 ₁₀	5 ₂	3 ₆	1 ₄	4 ₄	3 ₁₂	2 ₈	1 ₁₀	1 ₁₂	35	-2	-70	140
20-24	1 ₃	4 ₈	6 ₆	6 ₁	2 ₂	1 ₂	2 ₆	2 ₈	2 ₁₀	1 ₆		27	-1	-27	27
25-29	1	2	11	8	4	1	2	2	3			34		-213	
30-34	4 ₁₂	3 ₆	7 ₇	4	2	4	9 ₂₇			1 ₆	1 ₇	38	+1	+38	38
35-39	3 ₁₈	2 ₂₄	5 ₁₀	2	5 ₁₀	1 ₄	1 ₆	2 ₁₆	3 ₃₀	1 ₁₂		29	+2	+58	116
40-44	3 ₃₆	3 ₃₀	6 ₁₈	2	4 ₁₂	1 ₁₂	9 ₂₇	1 ₁₂	1 ₁₅			26	+3	+78	234
45-49	3 ₆₀	2 ₂₄	4 ₁₆	3	3 ₁₂	8 ₈	1 ₁₆					20	+4	+80	320
50-54	1 ₁₅		5 ₅									3	+5	+15	75
f	20	34	51	36	28	16	21	18	13	4	1	241		369	1430
d	-3	-2	-1	0	+1	+2	+3	+4	+5	+6	+7				
fd	-60	-68	-51	0	28	32	63	72	60	24	7	285			
fd²	180	136	51	0	28	64	189	288	300	144	49	1430			

$$(z = xy) = -258$$



Correlações parciais

Estatística = 1
Matemática = 2
M. Mental = 3

$$\sqrt{r_{2,3}} = \frac{0,150 - (0,050 \times 0,150)}{\sqrt{0,997500} \sqrt{0,977500}} =$$

$$= \frac{0,150 - 0,007500}{0,998 \times 0,988} =$$

$$= \frac{0,142500}{0,986024} = 0,144$$

$$\sqrt{r_{1,2}} = \frac{0,050 - (0,150 \times 0,150)}{\sqrt{0,977500} \sqrt{0,977500}} =$$

$$= \frac{0,050 - 0,022500}{0,988 \times 0,988} =$$

$$= \frac{0,027500}{0,974500} = 0,028$$

$$\sqrt{r_{2,1}} = \frac{0,150 - (0,150 \times 0,050)}{\sqrt{0,972500} \sqrt{0,997500}} =$$

$$= \frac{0,150 - 0,007500}{0,988 \times 0,998} =$$

$$= \frac{0,142500}{0,986024} = 0,144$$

Erros padrões

$$\sigma_{r_{1,3}} = \frac{1 - 0,144^2}{\sqrt{77}} = \frac{1 - 0,020736}{8,77} = \frac{0,979264}{8,77} =$$

$$= 0,111$$

$$\sigma_{r_{1,2}} = \frac{1 - 0,028^2}{\sqrt{77}} = \frac{1 - 0,000784}{8,77} = \frac{0,999216}{8,77} =$$

$$= 0,113$$

$$\sigma_{r_{2,3,1}} = \frac{1 - 0,144^2}{\sqrt{77}} = \frac{1 - 0,020736}{8,77} = \frac{0,979264}{8,77} =$$

$$= 0,111$$

Estatístico - Auxiliar

(2º concurso)

Candidatos aprovados

Correlações simples

Variáveis	N	\bar{r}	$\sigma_{\pm r}$
Est. x Mat.	77	0,150	0,111
N.M. x Mat.	77	0,150	0,111
N.M. x Est.	77	-0,050	0,113
N.M. x Port.	77	0,125	0,112
Mat. x Port.	77	0,100	0,112
Est. x Port.	77	0,225	0,108

Correlações parciais

Variáveis	r	σ_{\pm}
Est. x Mat.	0,144	0,111
N.M. x Est.	0,028	0,113
Mat. x N.M.	0,144	0,111

Português = variável x Variável y

	40-44	45-49	50-54	55-59	60-64	65-69	70-74	75-79	f	d	fd	fd ²
60-64	1 8	2 12	3 12		29	7 14			42	-2	-84	168
65-69		1 3	3 12	1 1	8	2 1	16		12	-1	-12	12
70-74			1 1	1 1	2	1 1			12		-96	
75-79					5	1 1			6	+1	+6	6
80-84					1	4 4	6		3	+2	+6	12
85-89					2				2	+3	+6	18
f	1	3	4	2	55	11	2	1	N=77		18	216
d	-4	-3	-2	-1		+1	+2	+3				
fd	-4	-9	-8	-2		+11	4	3	18			
fd ²	16	27	16	2		11	8	9	89			

$$\sigma_x = \frac{1 - 0,225^2}{\sqrt{77}} = \frac{1 - 0,050625}{8,77} = \frac{0,949375}{8,77} = \pm 0,108$$

$$= \frac{0,949375}{8,77} = \pm 0,108$$

$$c = \frac{-78}{77} \times 5 = -1,012 \times 5 = -5,060$$

$$M = 72,5 - 5,060 = 67,440$$

$$\sigma = 5 \sqrt{\frac{216}{77} - 1,012^2} = 5 \times 1,334 = 6,670$$

$$c.v. = \frac{6,670}{67,440} \times 100 = 9,8$$

Variável x

$$c = \frac{-5}{77} \times 5 = -0,064 \times 5 = -0,320$$

$$M = 62,5 - 0,320 = 62,180$$

$$\sigma = 5 \sqrt{\frac{89}{77} - 0,064^2} = 5 \times 1,072 = 5,360$$

$$c.v. = \frac{5,360}{62,180} \times 100 = 8,6$$

Coefficiente de correlação

$$r = \frac{\frac{31}{77} - (1,012 \times 0,064)}{6,670 \times 5,360} \times 25 =$$

$$= \frac{0,402 - 0,064768}{35,751200} \times 25 =$$

$$= \frac{0,337232}{35,751200} \times 25 =$$

$$= 0,009 \times 25 = \underline{0,225}$$

Português = variável x

	40-44	45-49	50-54	55-59	60-64	65-69	70-74	75-79	f	d	fd	fd ²
60-64	1 ₁₂	3 ₁₈	2 ₁₂		25	4 ₁₂			34	-3	-102	306
65-69		1 ₆	5 ₃₀	1 ₅	5	3 ₆	1 ₄	2 ₄	11	-2	-22	44
70-74				1 ₁	4	2 ₁			4	-1	-4	7
75-79			1		9	1	1		12		-131	
80-84					4		1 ₂		5	+1	+5	5
85-89			6				5		2	+2	+4	8
90-94		1 ₆				1 ₃	3 ₃		5	+3	+15	45
95-100									1	+4	+4	16
f	1	3	4	2	53	11	2	1	N=77		28	431
d	-4	-3	-2	-1		+1	+2	+3				
fd	-4	-9	-8	-2		+11	4	3	18			
fd ²	16	27	16	2		11	8	9	89			

$$\sigma_x = \frac{1 - 0,100}{\sqrt{77}} = \frac{1 - 0,010}{8,77} = \frac{0,990}{8,77} = \pm 0,112$$

Variável y

$$c = \frac{-103}{77} \times 5 = -1,337 \times 5 = -6,685$$

$$M = 77,5 - 6,685 = 70,815$$

$$\sigma = 5 \sqrt{\frac{431}{77} - 1,337^2} = 5 \times 1,951 = 9,755$$

$$O.V. = \frac{9,755}{70,815} \times 100 = 13,7$$

Variável x

$$c = \frac{-5}{77} \times 5 = -0,064 \times 5 = -0,320$$

$$M = 62,5 - 0,320 = 62,180$$

$$\sigma = 5 \sqrt{\frac{89}{77} - 0,064^2} = 5 \times 1,072 = 5,360$$

$$O.V. = \frac{5,360}{62,180} \times 100 = 8,6$$

Coefficiente de correlação

$$r = \frac{\frac{26}{77} - (-1,337 \times 0,064)}{9,755 \times 5,360} \times 25 =$$

$$= \frac{0,337 - 0,085568}{52,286800} \times 25 =$$

$$= \frac{0,251432}{52,286800} \times 25 =$$

$$= 0,004 \times 25 = 0,100$$

Português = variável x Variável y nível mental = variável y

	40-44	45-49	50-54	55-59	60-64	65-69	70-74	75-79	f	d	fd	fd²
55-59			1 10						1	-5	-5	25
60-64		1 12			1		1 8		3	-4	-12	48
65-69			2 9		4			1 3	4	-3	-12	36
70-74		X			4	1 2			5	-2	-10	20
75-79	1 4		1 2	1 1	4			1 3	8	-1	-8	8
80-84		1	1	1	13	6			22		-44	
85-89		1 3	1 2			3			14	+1	+14	14
90-94			1 5		5		1 4	1 10	14	+2	+28	56
95-100					5	1 3	X		6	+3	+18	54
f	1	3	4	2	23	11	2	1	N=74		60	261
d	-4	-3	-2	-1	0	+1	+2	+3				
fd	-4	-9	-8	-2	0	+11	+4	+3	18		-5	
fd²	16	27	16	2	0	11	8	9	89			

$$\sigma = \frac{1-0,150}{\sqrt{77}} = \frac{1-0,045625}{8,577} = \frac{0,954375}{8,577} = \pm 0,112$$

$$c = \frac{18}{77} \times 5 = 0,168 \times 5 = 0,840$$

$$M = 82,5 + 0,840 = 83,340$$

$$\sigma = 5 \sqrt{\frac{261}{77} - 0,168^2} = 5 \times 1,833 = 9,165$$

$$C.V. = \frac{9,165}{83,340} \times 100 = 10,9$$

Variável x

$$c = \frac{-5}{77} \times 5 = -0,064 \times 5 = -0,320$$

$$M = 62,5 - 0,320 = 62,180$$

$$\sigma = 5 \sqrt{\frac{89}{77} - 0,064^2} = 5 \times 1,072 = 5,360$$

$$C.V. = \frac{5,360}{62,180} \times 100 = 8,6$$

Coeficiente de correlação

$$r = \frac{-24}{44} - (0,168 \times 0,064) \times 25 =$$

$$= \frac{0,272 + 0,010752}{49,124400} \times 25 =$$

$$= \frac{0,282752}{49,124400} \times 25 =$$

$$= 0,005 \times 25 = \underline{0,125}$$

Estatística = variável x

Variável y

	60-64	65-69	70-74	75-79	80-84	85-89	90-94	95-100	f	d	fd	fd ²
55-59	1 10								1	-5	-5	25
60-64	1 8				1 8				3	-4	-12	48
65-69	2 12	3 6		1 3		1 3			4	-3	-12	36
70-74	3 12	1 4	2 2						5	-2	-10	20
75-79	1 2	3 3	1 1		1 2				8	-1	-8	8
80-84	10 10			3 3		1 1			22		-44	
85-89	1 14	2 2				1 3			14	+1	+14	14
90-94	6 24	3 6	1 1	2 2	1 4				14	+2	28	56
95-100	5 20			1 3		X 2			6	+3	18	54
f	42	12		6	3	2	-	-	N=77		60	261
d	-2	-1		+1	+2	+3	-	-				
fd	-84	-12		+6	6	6	-	-	18			
fd ²	168	12		6	12	18	-	-	216			

$$\sigma = \frac{1 - 2,025}{\sqrt{77}} = \frac{1 - 2,002500}{8,77} = \frac{2,224500}{8,77} = \pm 0,113$$

$$\Sigma(xy) = -25$$

$$c = \frac{13}{77} \times 5 = 0,168 \times 5 = 0,840$$

$$M = 82,5 + 0,840 = 83,340$$

$$\sigma = 5 \sqrt{\frac{261}{77} - 0,168^2} = 5 \times 1,833 = 9,165$$

$$C.V. = \frac{9,165}{83,340} \times 100 = 10,9$$

Variável x

$$c = \frac{-78}{77} \times 5 = -1,012 \times 5 = -5,060$$

$$M = 72,5 - 5,060 = 67,440$$

$$\sigma = 5 \sqrt{\frac{216}{77} - 1,012^2} = 5 \times 1,334 = 6,670$$

$$C.V. = \frac{6,670}{67,440} \times 100 = 9,8$$

Coeficiente de correlação

$$r = \frac{\frac{-2,5}{77} - (0,168 \times 1,012)}{9,165 \times 6,670} \times 25 =$$

$$= \frac{-0,324 + 0,170016}{61,130550} \times 25 =$$

$$= \frac{-0,153984}{61,130550} \times 25 =$$

$$= -0,002 \times 25 = -0,050$$

Matemática - variável x

	60-64	65-69	70-74	75-79	80-84	85-89	90-94	95-100	f	d	fd	fd²
55-59	1 15								1	-5	-5	25
60-64	1 12	2 16							3	-4	-12	48
65-69	1 9	X		2	1 3		3		4	-3	-12	36
70-74	2 12	2 8	1 2						5	-2	-10	20
75-79	4 12		2 2						8	-1	-8	8
80-84							1	1	22		-47	
85-89	6 18		1		1 4	2 6			14	+1	+14	14
90-94	9 54	2 16			4	3 6			14	+2	28	56
95-100	2 12				3	X 18			6	+3	18	54
f	34	16	3		5	2	5	1	N=77		60	261
d	-5	-2	-4		+1	+2	+3	+4				
fd	-15	-8	-12		5	4	15	4				
fd²	25	4	16		5	8	45	16				

$$\sigma_x = \frac{1 - 2,150^2}{\sqrt{77}} = \frac{1 - 0,222500}{8,77} = \frac{0,777500}{8,77} = \pm 0,111$$

Variável y

$$c = \frac{13}{77} \times 5 = 0,168 \times 5 = 0,840$$

$$M = 82,5 + 0,840 = 83,340$$

$$\sigma = 5 \sqrt{\frac{261}{77} - 0,168^2} = 5 \times 1,833 = 9,165$$

$$c.v. = \frac{9,165}{83,340} \times 100 = 10,9$$

Variável x

$$c = \frac{-103}{77} \times 5 = -1,337 \times 5 = -6,685$$

$$M = 77,5 - 6,685 = 70,815$$

$$\sigma = 5 \sqrt{\frac{431}{77} - 1,337^2} = 5 \times 1,951 = 9,755$$

$$c.v. = \frac{9,755}{70,815} \times 100 = 13,7$$

Coeficiente de correlação

$$r = \frac{\frac{28}{77} - (0,168 \times 1,337)}{9,165 \times 9,755} \times 25 =$$

$$= \frac{0,363 + 0,224616}{89,404575} \times 25 =$$

$$= \frac{0,587616}{89,404575} \times 25 =$$

$$= 0,006 \times 25 = 0,150$$

Matemática = variável x

	60-64	65-69	70-74	75-79	80-84	85-89	90-94	95-100	f	d	fd	fd²
60-64	22 132	6 24	3 6	5 15	1 4	1 4	3 18	1 8	42	-2	-84	168
65-69	4 12	2 6	2 6	3 9	1 4	1 4	3 18	1 8	12	-1	-12	12
70-74	6 18	2 6	1 3	2 6	2 6	1 3	1 3	1 3	12	0	0	0
75-79	1 3	1 3	2 6	1 3	1 3	1 3	3 9	1 3	6	+1	+6	6
80-84	1 3	1 3	1 3	1 3	1 3	1 3	1 3	1 3	3	+2	+6	12
85-89	1 3	1 3	1 3	1 3	1 3	1 3	1 3	1 3	2	+3	+6	18
f	34	11	7	12	5	2	5	1	77			
d	-3	-2	-1	0	+1	+2	+3	+4				
fd	102	22	7	15	5	4	15	4				
fd²	306	44	7	15	5	8	45	16				

$$\sigma_x = \frac{1-0,150^2}{\sqrt{77}} = \frac{1-0,0225}{8,77} = \frac{0,9775}{8,77} = 0,111$$

Variável y

$$c = \frac{-78}{77} \times 5 = -1,012 \times 5 = -5,060$$

$$M = 72,5 - 5,060 = 67,440$$

$$\sigma_y = 5 \sqrt{\frac{216}{77} - 1,012^2} = 5 \times 1,334 = 6,670$$

$$C.V. = \frac{6,670}{67,440} \times 100 = 9,8$$

Variável x

$$c = \frac{-103}{77} \times 5 = -1,337 \times 5 = -6,685$$

$$M = 77,5 - 6,685 = 70,815$$

$$\sigma_x = 5 \sqrt{\frac{454}{77} - 1,337^2} = 5 \times 1,951 = 9,755$$

$$C.V. = \frac{9,755}{70,815} \times 100 = 13,7$$

Coefficiente de correlação

$$r = \frac{\frac{136}{77} - (1,012 \times 1,337)}{6,670 \times 9,755} \times 25 =$$

$$= \frac{1,766 - 1,353044}{65,065850} \times 25 =$$

$$= \frac{0,412956}{65,065850} \times 25 =$$

$$= 0,006 \times 25 = \underline{0,150}$$

Estadística Auxiliar (1º curso)

4ª Parte = variável x

	0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	f	d	fd	fd²
0-1	90	15	3	10				12			30	-3	-90	270
2-3		12	6	3	4			4			15	-2	-30	60
4-5		9	8	5	5	18		20			50	-1	-50	50
6-7			6	9	21	34	5				49			
8-9		3	9	1	3	35	51	5	10		98	+1	+98	98
10-11			6	8	10	43	51	9	2		91	+2	+182	364
12-13							39	12			17	+3	+51	153
14-15							4				1	+1	+4	16
f	23	17	22	110	176	21	335	21			335			1011
d	-3	-2	-1		+1	+2								
fd	-69	-34	-21		+176	+42								
fd²	207	68	21		176	84								

5ª Parte = variável y

$$\Sigma(xy) = 341$$

Variável y

$$c = \frac{165}{381} \times 2 = 0,433 \times 2 = 0,866$$

$$M = 7 + 0,866 = 7,866$$

$$\sigma = 2 \sqrt{\frac{1011}{381} - 0,433^2} = 2 \times 1,570 = 3,140$$

$$C.V. = \frac{3,140}{7,866} \times 100 = 39,9$$

Variável x

$$c = \frac{87}{381} \times 2 = 0,228 \times 2 = 0,456$$

$$M = 7 + 0,456 = 7,456$$

$$\sigma = 2 \sqrt{\frac{563}{381} - 0,228^2} = 2 \times 1,193 = 2,386$$

$$C.V. = \frac{2,386}{7,456} \times 100 = 32$$

Coefficiente de correlação

$$r = \frac{341}{381} - (0,433 \times 0,228) \times 4 =$$

$$= \frac{0,895 - 0,098724}{7,492040} \times 4 =$$

$$= \frac{0,796276}{7,492040} \times 4 =$$

$$= 0,106 \times 4 = 0,424$$

$$r_c = \frac{1 - 0,424^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,179776}{19,51} =$$

$$= \frac{0,820224}{19,51} = 0,042$$

Estadística Auxiliar (1º. semestre)

3ª Parte = variável x

	0-2	3-5	6-8	9-11	12-14	15-17	18-20	21-23	24-26	27-29	30-32	33-35	36-38	39-41	f	d	fd	fd²
0-1	8 168 21		2 30 15		2 18 9		1 3 3	1		5 30 6	11 99 9				30	-3	-90	270
2-3	1 14 14	2 24 12		1 18 9		1 4 4	1 2 2		2 4 2	8 8 4	5 50 6				15	-2	-30	60
4-5	10 70 7	3 18 6		1 4 4	2 6 3	2 4 2	2 2 1	3	3 3 1	11 22 2	13 39 3				50	-1	-50	50
6-7	12 72 6	5 30 5	3 15 5		4 20 4			2	4 20 4	12 60 6	29 145 9				49	0	-140	
8-9	10 70 7	3 18 6	3 15 5	2 10 5	1 6 3	1 4 2	2 12 4	4	11 55 11	10 50 5	47 235 11		1 6 6		98	+1	+98	98
10-11	2 14 14	2 12 6	1 6 3	5 30 6	1 6 3	3 12 4	4 20 4	1	4 20 4	14 70 7	54 270 9				91	+2	+182	364
12-13	1 7 7		1 6 3												17	+3	+51	153
14-15		1 7 7													1	+4	+4	16
f	44	16	10	14	10	10	10	11	27	57	141	-	-	1	335			1011
d	-7	-6	-5	-4	-3	-2	-1		+1	+2	+3	-	-	+6				
fd	-308	-36	-50	-56	-30	-20	-10	-570	+27	+114	+513	-	-	6	660			
fd²	2156	576	250	224	90	40	10		27	228	1539	-	-	36	5176			

$$\Sigma = (xy) = 520$$

Variável y

$$c = \frac{165}{381} \times 2 = 0,433 \times 2 = 0,866$$

$$M = 7 + 0,866 = 7,866$$

$$\sigma = 2 \sqrt{\frac{1011}{381} - 0,433^2} = 2 \times 1,570 = 3,140$$

$$C.V. = \frac{3,140}{7,866} \times 100 = 39,9$$

Variável x

$$c = \frac{90}{381} \times 3 = 0,236 \times 3 = 0,708$$

$$M = 22,5 + 0,708 = 23,208$$

$$\sigma = 3 \sqrt{\frac{5176}{381} - 0,236^2} = 3 \times 3,648 = 10,934$$

$$C.V. = \frac{10,934}{23,208} \times 100 = 47,5$$

Coefficiente de correlação

$$r = \frac{520}{381} - (0,433 \times 0,236) \times 6 = \frac{1,364 - 0,103188}{34,646760} \times 6 =$$

$$= \frac{1,261812}{34,646760} \times 6 =$$

$$= \frac{1,261812}{34,646760} \times 6 =$$

$$= 0,036 \times 6 = 0,216$$

$$\sigma_r = \frac{1 - 0,216^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,046656}{19,51} =$$

$$= \frac{0,953344}{19,51} = \pm 0,048$$

Estatístico-Auxiliar (comum)

4ª Parte = variável x

	0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	f	d	fd	fd²
0-2	11	23	2	4	28	15	11	1	14	44	44	-7	-308	2156
3-5				3	18	7	6		36	16	16	-6	-96	576
6-8	3	45				3	4		20	10	10	-5	-50	250
9-11	1	12	16	2	8	4	5		20	14	14	-4	-56	224
12-14			24	6	3	3	2		6	10	10	-3	-30	90
15-17	2	12		1	2	4	3		6	10	10	-2	-20	40
18-20	1	3	1	2	2	4	2		2	10	10	-1	-10	10
21-23			1	2	5	3				11	11			
24-26	2	6		5	5	10	12	1	2	24	24	+1	+24	24
27-29	3	18	2	3	6	18	30	1	4	57	57	+2	+114	228
30-32			5	30	15	26	77	12	108	141	141	+3	+513	1539
33-35														
36-38														
39-41														
f	23	14	28	116	116	21	81			560	560			5176
d	-3	-2	-1			+1	+2							
fd	-69	-28	-28			+21	+136			218	218			
fd²	207	112	28			21	178			563	563			

Variável y

$$c = \frac{90}{381} \times 3 = 0,236 \times 3 = 0,708$$

$$M = 22,5 + 0,708 = 23,208$$

$$\sigma = 3 \sqrt{\frac{5176}{381} - 0,236^2} = 3 \times 3,678 = 11,034$$

$$C.V. = \frac{11,034}{23,208} \times 100 = 47,5$$

Variável x

$$c = \frac{87}{381} \times 2 = 0,228 \times 2 = 0,456$$

$$M = 7 + 0,456 = 7,456$$

$$\sigma = 2 \sqrt{\frac{563}{381} - 0,228^2} = 2 \times 1,193 = 2,386$$

$$C.V. = \frac{2,386}{7,456} \times 100 = 32$$

Coefficiente de variação

$$u = \frac{648}{381} - (0,236 \times 0,228) \times 6 =$$

$$= \frac{1700 - 0,053808}{26,327124} \times 6 =$$

$$= \frac{1,646192}{26,327124} \times 6 =$$

$$= 0,062 \times 6 = 0,372$$

$$\sigma_n = \frac{1 - 0,372^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,138384}{19,51} =$$

$$= \frac{0,861616}{19,51} = 0,044$$

Estatística Auxiliar 1ª (comuns)

2ª Parte = variável x

	0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	18-19	19-20	20-21	21-22	22-23	23-24	24-25	25-26	26-27	27-28	28-29	29-30	f	d	fd	fd²
0-1	4	60	5	12	27	12	5	15	4	3	9	1	6	18	1	12															30	-3	-90	270
2-3	2	10	2	16	8	8	4	4	3	1	2	1	4	4	4	8															15	-2	-30	60
4-5	2	10	4	16	9	9	18	10	10	7	4	5	10	6	6	6														10	50	-1	-50	50
6-7	3	8	8	8	4	14	10	10	14	14	8	5	2																		79		-170	
8-9	2	10	3	12	8	24	13	11	14	16	16	22	6	18	3	12															98	+1	+98	98
10-11	2	10	2	16	4	24	8	8	14	14	20	12	4	12	4	12															91	+2	+182	364
12-13																															17	+3	+51	153
14-15																															1	+4	+4	16
f	15	24	26	43	64	64	53	61	30	17	-	-	-	-	-	1														381		335	1011	
d	-5	-4	-3	-2	-1		+1	+2	+3	+4	-	-	-	-	-	+10																		
fd	-75	-96	-78	-86	-64	-389	+53	+122	+90	+68	-	-	-	-	-	10															343		-46	
fd²	275	384	234	148	64		53	244	270	272	-	-	-	-	-	100															2158			

Variável y

$$\sigma = \frac{165}{381} \times 2 = 0,433 / 2 = 0,2165$$

$$M = 7 + 0,266 = 7,266$$

$$\sigma = 2 \sqrt{\frac{1011}{381} - 0,433^2} = 2 \times 1,580 = 3,16$$

$$C.V. = \frac{3,16}{7,266} \times 100 = 39,9$$

Variável x

$$\sigma = \frac{46}{381} \times 2 = 0,20 \times 2 = 0,240$$

$$M = 11 - 0,240 = 10,760$$

$$\sigma = 2 \sqrt{\frac{2158}{381} - 0,120^2} = 2 \times 2,376 = 4,752$$

$$C.V. = \frac{4,752}{10,760} \times 100 = 44,1$$

Coefficiente de correlação

$$r = \frac{380}{381} - (0,433 \times 0,120) \times 4 = \frac{380}{381} - 0,051960 \times 4 = \frac{1,048960}{14,921380} \times 4 = 0,070 \times 4 = 0,280$$

$$\sigma_r = \frac{1 - 0,280^2}{\sqrt{381}} = \frac{1 - 0,078400}{19,51} = \frac{0,921600}{19,51} = \pm 0,047$$

Estadística - Auxiliar (1º Curso)

2ª Parte = variável x

0-1	2-3	4-5	6-7	8-9	10-11	12-13	14-15	16-17	18-19	20-21	22-23	24-25	26-27	28-29	30-31	f	d	fd	fd²
3 45	5 60	3 24	4 24	4 12	2		1 6	1 9								23	-3	-69	207
2 20	3 24	1 6	2 8	5 10		3 6			1 8							17	-2	-34	68
3 15	2 8	3 9	4 14	6 6	3	1 1	2 4	1 3								28	-1	-28	28
6 10	10 13	13 15	15 16	16 23	23	15	12	4	2							116	0	-131	
1 5	4 16	6 18	14 28	23 23	27	31	43	16 48	10 40						10	176	+1	+176	176
			4		2	3	3	8 48	4 32						10	21	+2	42	84
15	24	26	43	54	57	53	61	30	14	-	-	-	-	-	1	381		218 = 87	563
-5	-4	-3	-2	-1	0	+1	+2	+3	+4	-	-	-	-	-	+10				
-75	-96	-78	-86	-54	-381	+63	122	90	68	-	-	-	-	-	10	393		-46	
375	384	234	172	54		53	249	270	342	-	-	-	-	-	100	2158			

1ª Parte = variável y

$$\sum (x \cdot y) = 470$$

Variável y

$$c = \frac{87}{381} \times 2 = 0,228 \times 2 = 0,456$$

$$M = 7 - 0,456 = 6,544$$

$$\sigma = 2 \sqrt{\frac{563}{381} - 0,228^2} = 2 \times 1,193 = 2,386$$

$$C.V. = \frac{2,386}{6,544} \times 100 = 36,46$$

Variável x

$$c = \frac{-46}{381} \times 2 = -0,120 \times 2 = -0,240$$

$$M = 11 - 0,240 = 10,760$$

$$\sigma = 2 \sqrt{\frac{2158}{381} - 0,120^2} = 2 \times 2,376 = 4,752$$

$$C.V. = \frac{4,752}{10,760} \times 100 = 44,16$$

Coefficiente de correlação

$$r = \frac{470}{381} - (0,228 \times 0,120) \times 4 = \frac{2,386 \times 4,752}{11,338272}$$

$$= \frac{1,260360}{11,338272} \times 4 =$$

$$= \frac{1,260360}{11,338272} \times 4 =$$

$$= 0,111 \times 4 = 0,444$$

$$\sigma_r = \frac{1 - 0,444^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,197136}{19,51} =$$

$$= \frac{0,802864}{19,51} = \pm 0,041$$

Estatístico-Auxiliar (1º semestre)

2ª Parte - variável x

	0-1	2-3	4-5	6-7	8-9	10-11	12-13	14-15	16-17	18-19	20-21	22-23	24-25	26-27	28-29	30-31	f	d	fd	fd ²
0-2	3 105	4 196	8 168	8 112	6 42	4	4 28	1 14	2 42	1 28							44	-7	-308	2156
3-5		2 48		2 24	3 18	3	4 24	1 12								1 60	16	-6	-96	576
6-8	1 25	1 20	1 15	2 20	4 20	1											10	-5	-50	250
9-11	2 40	1 16	2 24	2 16	2 8	3	1 4	1 8									14	-4	-56	224
12-14	1 15	2 24	2 18	1 6	1 3	1	1 3	1 6									10	-3	-30	90
15-17		1 8	2 12	1 4		6											10	-2	-20	40
18-20		1 4	2 6	3 6	1 1	1	2 2										10	-1	-10	10
21-23		1	1	3	1	1	3		1								11	0	-570	
24-26	1 5	1 4	1 3	4 8	3 3	4	4 4	7 14	1 3	1 4							27	+1	+27	27
27-29	2 20	1 8	1 6	7 28	15 30	3	11 22	7 28	4 24								57	+2	+114	228
30-32	5 75	6 72	6 54	10 60	18 54	11	23 69	42 252	22 198	15 180							141	+3	+513	1539
33-35																				
36-38																				
39-41																				
f	35	24	26	43	54	57	53	61	30	17	-	-	-	-	-	1	381	660	5176	
d	-5	-4	-3	-2	-1	0	+1	+2	+3	+4	-	-	-	-	-	+10				
fd	-175	-96	-78	-86	-54	-389	53	122	90	68	-	-	-	-	-	10	343	-46		
fd ²	375	256	234	172	84		53	244	270	272	-	-	-	-	-	100	2158			

$$c = \frac{30}{381} \times 3 = 0,236 \times 3 = 0,708$$

$$M = 22,5 + 0,708 \times 23,208$$

$$\sigma = 3 \sqrt{\frac{5176}{381} - 0,236^2} = 3 \times 13,678 = 41,034$$

$$C.V. = \frac{41,034}{23,208} \times 100 = 175,5$$

$$c = \frac{-46}{381} \times 2 = -0,120 \times 2 = -0,240$$

$$M = 11 - 0,240 = 10,760$$

$$\sigma = 3 \sqrt{\frac{2158}{381} - 0,120^2} = 3 \times 7,52 = 22,56$$

$$C.V. = \frac{22,56}{10,760} \times 100 = 210,1$$

$$r = \frac{2073 - (0,236 \times 3420)}{381} \times 6 = \frac{5,46 \times 320}{52,433568} \times 6 = 0,624$$

$$r = \frac{2073 - (0,236 \times 3420)}{381} \times 6 = \frac{5,46 \times 320}{52,433568} \times 6 = 0,624$$

$$r = \frac{5,46 \times 320}{52,433568} \times 6 = 0,624$$

$$r = 0,624 \times 6 = 0,624$$

$$r = 0,624 \times 6 = 0,624$$

$$r = \frac{1 - 0,624^2}{19,51} =$$

$$= \frac{1 - 0,389376}{19,51} =$$

$$= \frac{0,610624}{19,51} = \pm 0,030$$

5ª Parte - variável x

	0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	f	d	fd	fd²
0-1	4 60	15 10	8 40	3 15	2 10	2 10									20	-5	-100	500
2-3	6 72	12 16	8 32	8 32	6 24	2 16									32	-4	-128	512
4-5	5 45	9 18	6 24	5 20	5 25	1 6	1 6								19	-3	-57	171
6-7		8 32	4 16	5 20	6 24	2 16									11	-2	-22	44
8-9	4 12	3 9	5 15	6 18	6 18	2 6	1 3	1 3	4 12						25	-1	-25	25
10-11			6 18	10 30	13 39	6 18	1 3	1 3	4 12						34	0	-332	
12-13		3 9	6 18	4 12	10 30	13 39	11 33	1 3	3 9						43	+1	+43	43
14-15		2 6	3 9	2 6	11 33	18 54	20 60	1 3	6 18						60	+2	+120	240
16-17		2 6	1 3	18 54	15 45	19 57	6 18	9 27	12 36						58	+3	+171	522
18-19		2 6	16 48	20 60	18 54	19 57	6 18	8 24	12 36						62	+4	+248	992
20-21	1 3	15 45			20 60	18 54	9 27	10 30	15 45						47	+5	+235	1105
f	30	15	50	42	98	81	14	1	38						381		670	3474
d	-3	-2	-1	0	+1	+2	+3	+4										
fd	-90	-30	-50	-140	98	182	51	4	335									
fd²	270	60	50		98	364	153	16	1011									

Variável y

$$c = \frac{338}{381} \times 2 = 0,887 \times 2 = 1,774$$

$$M = 11 + 1,774 = 12,774$$

$$\sigma = 2 \sqrt{\frac{3474}{381} - 0,887^2} = 2 \times 2,886 = 5,772$$

$$C.Y. = \frac{5,772}{12,774} \times 100 = 45,1$$

Variável x

$$c = \frac{165}{381} \times 2 = 0,433 \times 2 = 0,866$$

$$M = 7 + 0,866 = 7,866$$

$$\sigma = 2 \sqrt{\frac{1011}{381} - 0,433^2} = 2 \times 1,570 = 3,140$$

$$C.Y. = \frac{3,140}{7,866} \times 100 = 39,9$$

Coeficiente de correlação

$$r = \frac{\frac{860}{381} - (0,887 \times 0,433)}{5,772 \times 3,140} \times 4 =$$

$$= \frac{2,257 - 0,384071}{18,124080} \times 4 =$$

$$= \frac{1,872929}{18,124080} \times 4 =$$

$$= 0,061 \times 4 = 0,103$$

$$\sigma_r = \frac{1 - 0,103^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,010609}{19,51} =$$

$$= \frac{0,989391}{19,51} = 0,050$$

4ª Parte = variável x

1ª Parte = variável y

	0-1	2-3	4-5	6-7	8-9	10-11	f	d	fd	fd²
0-1	4 60	3 30	1 5	7 20	5 20		20	-5	-100	500
2-3	5 60	4 32	2 8	12 36	9 36		32	-4	-128	512
4-5	3 27	2 12	2 8	5 20	6 18	1 6	19	-3	-57	171
6-7	1 6	4 16	3 12	3 12	3 12	1 6	11	-2	-22	44
8-9	3 9	2 8	4 16	7 28	9 36		25	-1	-25	25
10-11	2 6	1 4	5 20	14 56	11 44	1 6	34	0	-332	
12-13	2 6		5 20	19 76	17 68		43	+1	+43	43
14-15	2 6	3 12	4 16	16 64	8 32	4 16	60	+2	+120	240
16-17		1 4	3 12	10 40	10 40	6 36	58	+3	+174	522
18-19	1 6		4 16	15 60	9 36	1 6	62	+4	+248	992
20-21				9 36	4 16	1 6	17	+5	+85	425
f	23	17	28	46	176	21	381		670	3474
d	-3	-2	-1	0	+1	+2				
fd	-69	-34	-28	0	+176	+42				
fd²	207	68	28	0	176	84				

Variável y

$$c = \frac{338}{381} \times 2 = 0,887 \times 2 = 1,774$$

$$M = 11 + 1,774 = 12,774$$

$$\sigma = 2 \sqrt{\frac{3474}{381} - 0,887^2 \times 2 \times 2,886} = 5,772$$

$$C.V. = \frac{5,772}{12,774} \times 100 = 45,1$$

Variável x

$$c = \frac{84}{381} \times 2 = 0,228 \times 2 = 0,456$$

$$M = 7 + 0,456 = 7,456$$

$$\sigma = 2 \sqrt{\frac{563}{381} - 0,228^2 \times 2 \times 1,193} = 2,386$$

$$C.V. = \frac{2,386}{7,456} \times 100 = 32$$

Coefficiente de correlação

$$r = \frac{632}{381} - (0,887 \times 0,228) \times 4 =$$

$$= \frac{1,658 - 0,202236}{13,771992} \times 4 =$$

$$= \frac{1,455764}{13,771992} \times 4 =$$

$$= 0,105 \times 4 = 0,420$$

$$\sigma_r = \frac{1 - 0,420^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,176400}{19,51} =$$

$$= \frac{0,823600}{19,51} = \pm 0,042$$

Estadístico-Municipal (1º concurso)

3ª Parte = variável x

Variável y

$$c = \frac{287}{381} \times 3 = 0,753 \times 3 = 2,259$$

$$M = 10,5 + 2,259 = 12,759$$

$$\sigma = 3 \sqrt{\frac{1669}{381} - 0,753^2} = 3 \times 1,952 = 5,856$$

$$C.V. = \frac{5,856}{12,759} \times 100 = 45,8$$

Variável x

$$c = \frac{90}{381} \times 3 = 0,236 \times 3 = 0,708$$

$$M = 12,5 + 0,708 = 13,208$$

$$\sigma = 3 \sqrt{\frac{5146}{381} - 0,236^2} = 3 \times 5,678 = 17,034$$

$$C.V. = \frac{17,034}{13,208} \times 100 = 128,9$$

Coefficiente de correlação

$$r = \frac{\frac{1943}{381} - (0,753 \times 0,236)}{5,856 \times 17,034} \times 9 =$$

$$= \frac{2,2175 - 0,177708}{64,615104} \times 9 =$$

$$= \frac{2,294292}{64,615104} \times 9 =$$

$$= 0,315 \times 9 = 0,315$$

$$\sigma_r = \frac{1 - 0,315^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,099225}{19,51} =$$

$$= \frac{0,900775}{19,51} = \pm 0,041$$

1ª Parte = variável y

	0-2	3-5	6-8	9-11	12-14	15-17	18-20	21-23	24-26	27-29	30-32	33-35	36-38	39-41	f	d	fd	fd²
0-2	13 273	2 36	1 15	1 12	1 9	1 6	2 6		1 3	11 66	10 90				43	-3	-129	387
3-5	6 84		2 20	3 24	3 18			2		4 16	8 48				28	-2	-56	112
6-8	1 7	1 6		1 4	2 6		2 2	1	3 3	3 6	5 15				49	-1	-49	19
9-11	11 11	3 3	2 2	1 1	1 1	1 1	3 3	2	5 5	10 10	12 12				51	0	-204	
12-14	7 49	4 24	4 20	4 16	1 3	1 2	2 2	3	9 9	9 18	24 72				68	+1	+68	68
15-17	4 56	5 60	1 10	3 24	1 6	3 12	1 2	2	7 14	13 52	53 159				93	+2	+186	372
18-20	2 42	1 18		1 12	1 9	4 24		1	2 6	7 42	59 177			1 18	79	+3	+237	711
f	44	16	10	14	10	10	10	11	27	57	171	-	-	1	381		491	1669
d	-7	-6	-5	-4	-3	-2	-1	0	+1	+2	+3	-	-	+6				
fd	-308	-96	-50	-56	-30	-20	-10	-570	+27	+114	+513	-	-	6	660			
fd²	2156	576	250	224	90	40	10		27	228	1539	-	-	36	5176			

$$\Sigma = (xy) = 943$$

Estadística Auxiliar (1º curso)

2ª Parte - variável x

Variável Y

	0-1	2-3	4-5	6-7	8-9	10-11	12-13	14-15	16-17	18-19	20-21	22-23	24-25	26-27	28-29	30-31	f	d	fd	fd²
0-1	6 150	4 80	2 30	4 40		2			1 15	1 20							20	-5	-100	500
2-3	3 60	7 112	5 60	4 32	7 28	4	2 8										32	-4	-128	512
4-5	2 30	2 24	3 27	2 12	4 12	2	2 6	2 12			28						19	-3	-57	171
6-7	1 10	3 24	X		2 4	2	2 4		1 6								11	-2	-22	44
8-9	1 5	1 4	5 15	9 18	3 3	1	1 1	3 6							1 10		25	-1	-25	25
10-11	2	1	5	6	7	6	2	4	1								34		-332	
12-13		4	3	6	9	5	9	9	2	1							43	+1	+43	43
14-15		3	4	6	9	10	15	9	3	1							60	+2	+120	240
16-17		2	2	5	9	12	9	10	7	4							58	+3	+174	522
18-19			1	1	3	9	8	21	11	7							62	+4	+248	992
20-21					5	4	2	3	1	3							17	+5	+85	435
f	15	24	26	43	54	57	53	61	30	17	-	-	-	-	-	1	381		670	3474
d	-5	-4	-3	-2	-1	-	+1	+2	+3	+4	-	-	-	-	-	+10				
fd	-25	-24	-39	-26	-54	-383	+53	+122	+90	+68	-	-	-	-	-	10	343		-46	
fd²	125	136	231	132	274	1459	53	244	270	272	-	-	-	-	-	100	2158			

$$\sigma = \frac{338}{381} \times 12 = 0,887 \times 12 = 1,0644$$

$$M = 11 + 1,0644 = 12,0644$$

$$\sigma = 3 \sqrt{\frac{3474}{381} - 0,887^2} = 3 \sqrt{2,886} = 5,772$$

$$C.V. = \frac{5,772}{12,0644} \times 100 = 47,8$$

Variável x

$$\sigma = \frac{46}{381} \times 2 = 0,120 \times 2 = 0,240$$

$$M = 11 - 0,240 = 10,760$$

$$\sigma = 2 \sqrt{\frac{2158}{381} - 0,120^2} = 2 \sqrt{2,376} = 4,752$$

$$C.V. = \frac{4,752}{10,760} \times 100 = 44,1$$

Coefficiente de correlação

$$r = \frac{1391}{381} - (0,887 \times 0,120) \times 4 =$$

$$= \frac{3,650 + 0,106440 \times 4}{27,428544} =$$

$$= \frac{3,650 + 0,425760}{27,428544} \times 4 =$$

$$= 0,136 \times 4 = 0,544$$

$$\sigma_r = \frac{1 - 0,544^2}{\sqrt{381}} =$$

$$= \frac{1 - 0,295936}{19,51} =$$

$$= \frac{0,704064}{19,51} = \pm 0,036$$

$$\Sigma(x) = 1391$$

Correlações parciais

Estatística = 1

Matemática = 2

N. Mental = 3

$$r_{13.2} = \frac{0,250 - (0,250 \times 0,425)}{\sqrt{0,937500} \sqrt{0,819375}}$$

$$= \frac{0,250 - 0,106250}{0,968 \times 0,905} =$$

$$= \frac{0,143750}{0,876040} = 0,164$$

$$r_{12.3} = \frac{0,425 - (0,250 \times 0,250)}{\sqrt{0,937500} \sqrt{0,937500}}$$

$$= \frac{0,425 - 0,062500}{0,968 \times 0,968}$$

$$= \frac{0,362500}{0,937500} = 0,386$$

$$r_{23.1} = \frac{0,250 - (0,425 \times 0,250)}{\sqrt{0,937500} \sqrt{0,937500}}$$

$$= \frac{0,250 - 0,106250}{0,905 \times 0,968}$$

$$= \frac{0,143750}{0,876040} = 0,164$$

Erros padrões

$$\sigma_{r_{13.2}} = \frac{1 - 0,164^2}{\sqrt{124}} = \frac{1 - 0,026896}{11,13} = \frac{0,973104}{11,13} = 0,087$$

$$\sigma_{r_{12.3}} = \frac{1 - 0,386^2}{\sqrt{124}} = \frac{1 - 0,148996}{11,13} = \frac{0,851004}{11,13} = 0,076$$

$$\sigma_{r_{23.1}} = \frac{1 - 0,164^2}{\sqrt{124}} = \frac{1 - 0,026896}{11,13} = \frac{0,973104}{11,13} = 0,087$$

Concurso de Escriturário

(1º concurso)

Candidatos aprovados

Correlações simples

Variáveis	N	r	σ_r \pm
N.M. x Mat.	124	0,250	0,084
N.M. x Port.	124	0,175	0,087
N.M. x Est.	124	0,250	0,084
Mat. x Est.	124	0,425	0,073
Port. x Est.	124	0,150	0,087
Mat. x Port.	124	0,175	0,087

Correlações parciais

Variáveis	r	σ_r \pm
Est. x Mat.	0,386	0,076
N.M. x Est.	0,164	0,087
Mat. x N.M.	0,164	0,087

Aritmética = variável x

Variável y

Português = variável y

	50-54	55-59	60-64	65-69	70-74	75-79	80-84	85-89	90-94	f	d	fd	fd ²
60-64	12	96	48	120	14	13	9	3	100	83	-2	166	332
65-69	1	4	12	6	4	8	6	5	10	32	-1	32	32
70-74				1		1				2	0	-198	
75-79	1	4	1	2	6	1	1	1	3	6	+1	6	6
80-84								1	6	1	+2	2	4
f	14	13	13	15	36	21	14	5	2	N=124		8	374
d	-4	-3	-2	-1	0	+1	+2	+3	+4				
fd	56	39	26	16	-137	21	28	15	8				
fd ²	224	117	52	16		21	56	45	32				

$$s_x = \frac{1 - 0,175^2}{124} = \frac{1 - 0,030625}{11,13} = \frac{0,969375}{11,13} = \pm 0,087$$

$$\sum(xy) = 140$$

$$c = \frac{-190 \times 5}{124} = -1,532 \times 5 = -7,660$$

$$M = 72,5 - 7,660 = 64,840$$

$$s = 5 \sqrt{\frac{374}{124} - 1,532^2} = 5 \times 0,817 = 4,085$$

$$C.V. = \frac{4,085}{64,840} = 6,3$$

Variável x

$$c = \frac{-65}{124} \times 5 = -0,524 \times 5 = -2,620$$

$$M = 72,5 - 2,620 = 69,880$$

$$s = 5 \times \sqrt{\frac{563}{124} - 0,524^2} = 5 \times 2,065 = 10,325$$

$$C.V. = \frac{10,325}{69,880} = 14,7$$

Coefficiente de correlação

$$r = \frac{\frac{140}{124} - (-1,532 \times -0,524)}{4,085 \times 10,325} \times 25 =$$

$$= \frac{1,129 - 0,802768}{42,174625} \times 25 =$$

$$= \frac{0,326232}{42,174625} \times 25 =$$

$$= 0,007 \times 25 = 0,175$$

Estadística - variável x

Variável y

	35-39	40-44	45-49	50-54	55-59	60-64	65-69	70-74	75-79	80-84	85-89	90-94	95-100	f	d	fd	fd²
60-64	1	5	8	12	10	9	8	10	6	3	1	1	14	83	-2	-166	332
65-69	5	4	3	4	4	3	3	6	2	1	1	2	14	32	-1	-32	32
70-74					1		1							2		-198	
75-79			3			1	1	2				1	6	6	+1	+6	6
80-84		3							1	10				1	+2	2	4
f	2	6	10	13	16	16	13	17	12	8	5	3	3	N=124		8	374
d	-5	-4	-3	-2	-1		+1	+2	+3	+4	+5	+6	+7				
fd	-10	-24	-30	-26	-16		+13	+34	+36	32	25	18	21	179			
fd²	50	96	90	52	16		13	68	108	128	125	108	147	1001			

$$\sigma_x = \frac{1 - 0,150^2}{\sqrt{124}} = \frac{1 - 0,0225}{\sqrt{124}} = \frac{0,9775}{11,13} = 0,087$$

$$\Sigma = (\Sigma cy) = -68$$

$$= \pm 0,087$$

$$c = \frac{-190}{124} \times 5 = -1,532 \times 5 = -7,660$$

$$M = 72,5 - 7,660 = 64,840$$

$$\sigma = 5 \sqrt{\frac{374}{124} - 1,532^2} = 5 \times 0,817 = 4,085$$

$$c.v. = \frac{4,085}{64,840} = 6,3$$

Variável x

$$c = \frac{73}{124} \times 5 = 0,588 \times 5 = 2,940$$

$$M = 62,5 + 2,940 = 65,440$$

$$\sigma = 5 \sqrt{\frac{1001}{124} - 0,588^2} = 5 \times 2,779 = 13,895$$

$$c.v. = \frac{13,895}{65,440} = 21,2$$

Coefficiente de correlação

$$r = \frac{-68}{124} - \frac{(-1,532 \times 0,588)}{4,085 \times 13,895} \times 25 =$$

$$= \frac{-0,548 + 0,900816}{56,761075} \times 25 =$$

$$= \frac{-0,352816}{56,761075} \times 25 =$$

$$= 0,006 \times 25 = 0,150$$

Estatística = variável x

Variável y

	35-39	40-44	45-49	50-54	55-59	60-64	65-69	70-74	75-79	80-84	85-89	90-94	95-100	f	d	fd	fd ²
50-54		2	2	1	4	2	2		1					14	-1	-56	224
55-59	1	1	2	3	1	2			1	1				13	-3	-39	117
60-64	1	1	1	1	2	1	2		2	2				13	-2	-26	52
65-69		1	2	2	2	1			1	3		1		16	-1	-16	16
70-74			2	2	3	3	1	4	2	3			1	26	0	-137	
75-79		1	1	2	2	2	3	5	3	1	1			21	+1	+21	21
80-84				2	2	2	2	2	2	1		1		14	+2	+28	56
85-89								1	6	12	2	1		5	+3	+15	45
90-94								1	8	12		1		28	+4	+8	32
f	2	6	10	13	16	14	13	17	12	8	5	3	3	N=124		72	563
d	-5	-4	-3	-2	-1	0	+1	+2	+3	+4	+5	+6	+7				
fd	-10	-24	-30	-26	-16	-10	+13	34	26	32	25	18	21	179			
fd ²	50	96	90	52	16		13	68	108	128	125	108	147	1001			

$$\sigma_x = \frac{1 - 0,425^2}{\sqrt{124}} = \frac{1 - 0,180625}{11,13} = \frac{0,819375}{11,13} = 0,073 \approx (xy) = 2,67$$

$$c = \frac{-65}{124} \times 5 = -0,524 \times 5 = -2,620$$

$$M = 72,5 - 2,620 = 69,880$$

$$\sigma = 5 \sqrt{\frac{563}{124} - 0,524^2} = 5 \times 2,065 = 10,325$$

$$c.v. = \frac{10,325}{69,880} = 14,7$$

Variável x

$$c = \frac{73}{124} \times 5 = 0,588 \times 5 = 2,940$$

$$M = 62,5 + 2,940 = 65,440$$

$$\sigma = 5 \sqrt{\frac{1001}{124} - 0,588^2} = 5 \times 2,779 = 13,895$$

$$c.v. = \frac{13,895}{65,440} = 21,2$$

Coeficiente de correlação

$$r = \frac{2,67}{124} - \frac{(-0,524 \times 0,588)}{10,325 \times 13,895} \times 25 =$$

$$= \frac{2,153 + 0,308}{143,465875} \times 25 =$$

$$= \frac{2,461}{143,465875} \times 25 =$$

$$= 0,017 \times 25 = 0,425$$

Antecedente = variável y

Escriturário (1º concurso)

Candidatos aprovados

Estatística = variável x

Variável y

	35-39	40-44	45-49	50-54	55-59	60-64	65-69	70-74	75-79	80-84	85-89	90-94	95-100	f	d	fd	fd²
50-54						1	6							1	-6	-6	36
55-59		1	20				6							1	-5	-5	25
60-64					2	8	1			1	16			4	-4	-16	64
65-69			18		1	3	2	1		1	9			7	-3	-21	63
70-74		1	8	6	1	4	2	1	4		10			8	-2	-16	32
75-79	1	5	8	3	3	6	3	2	4		6			15	-1	-15	15
80-84	1					5	6	3	4	1	2	1		40	.	-79	
85-89		1	4	6	2	4	1	10	6	5	20			35	+1	+35	35
90-94			12		2		4	4	6	8	20	12	14	13	+2	26	52
95-100														-	-	-	-
f	2	6	10	13	16	16	13	14	12	8	5	3	3	N=124		61	322
d	-5	-4	-3	-2	-1		+1	+2	+3	+4	+5	+6	+7			± -18	
fd	-10	-24	-30	-26	-16	-10	+13	34	36	32	25	18	21	179		± -73	
fd²	50	96	90	82	16		13	68	108	128	125	108	147	1001			

$$\sigma_r = \frac{1 - 0,250^2}{\sqrt{124}} = \frac{1 - 0,0625}{11,13} = \frac{0,9375}{11,13} = 0,084$$

$$\Sigma = (\sigma_y) = 139$$

$$c = \frac{-18}{124} \times 5 = -0,145 \times 5 = -0,725$$

$$M = 82,5 - 0,725 = 81,775$$

$$\sigma = 5 \sqrt{\frac{322}{124} - 0,145^2} = 5 \times 1,604 = 8,020$$

$$c.v. = \frac{8,020}{81,775} = 9,8$$

Variável x

$$c = \frac{73}{124} \times 5 = 0,588 \times 5 = 2,940$$

$$M = 62,5 + 2,940 = 65,440$$

$$\sigma = 5 \sqrt{\frac{1001}{124} - 0,588^2} = 5 \times 2,779 = 13,895$$

$$c.v. = \frac{13,895}{65,440} = 21,2$$

Coefficiente de correlação

$$r = \frac{\frac{139}{124} - (0,145 \times 0,588)}{8,020 \times 13,895} \times 25 =$$

$$= \frac{1,120 + 0,085260 \times 25}{111,437900} =$$

$$= \frac{1,205260 \times 25}{111,437900} =$$

$$= 0,010 \times 25 = 0,250$$

Português = variável x Variável y .

	60-64	65-69	70-74	75-79	80-84	85-89	90-94	95-100	f	d	fd	fd^2
50-54	¹ +12								1	-6	-6	36
55-59	¹ +10								1	-5	-5	25
60-64	⁴ +32								4	-4	-16	64
65-69	⁵ +30	³ +3		¹ -3					7	-3	-21	63
70-74	⁵ +20	³ +6							8	-2	-16	32
75-79	¹⁰ +20	⁴ +4		¹ -1					15	-1	-15	15
80-84	²⁹	¹¹							40		-79	
85-89	²² -44	¹⁰ -10	²	¹ +1					35	+1	+35	35
90-94	⁶ -24	³ -6		³ +6	¹ +4				13	+2	+26	52
95-100									-	-	-	-
f	83	32	2	6	1	-	-	-	$N=124$		61	322
Σ	-3	-1		+1	+2						$\Sigma=18$	
fd	-66	-32	-18	+6	+4	-	-	-	8		$\Sigma=-190$	
fd^2	366	32		6	4	-	-	-	374			

$$C = \frac{-18}{124} \times 5 = -0,145 \times 5 = -0,725$$

$$M = 82,5 - 0,725 = 81,775$$

$$\sigma = 5 \sqrt{\frac{322}{124} - 0,145^2} = 5 \times 1,604 = 8,020$$

$$C.V. = \frac{8,020}{81,775} = 9,8$$

Variável x

$$C = \frac{-190}{124} \times 5 = -1,532 \times 5 = -7,660$$

$$M = 72,5 - 7,660 = 64,840$$

$$\sigma = 5 \sqrt{\frac{374}{124} - 1,532^2} = 5 \times 0,817 = 4,085$$

$$C.V. = \frac{4,085}{64,840} = 6,3$$

Coefficiente de correlação $\Sigma(xy) =$

60

$$r = \frac{\frac{60}{124} - (0,145 \times 1,532)}{8,020 \times 4,085} \times 25 =$$

$$= \frac{0,483 - 0,222140}{32,761700} \times 25 =$$

$$= \frac{0,260860}{32,761700} \times 25 = 0,007 \times 25 = 0,175$$

Aritmética - variável x

Variável y

	50-54	55-59	60-64	65-69	70-74	75-79	80-84	85-89	90-94	f	d	fd	fd²
50-54	1 24									1	-6	6	36
55-59	1 20									1	-5	5	25
60-64	1 16	1 12								4	-4	16	64
65-69	2 24	1 9	1 6	2 6	1 3					7	-3	21	63
70-74	1 8	1 6	2 8	1 4	1 2	2 4				8	-2	16	32
75-79	1 4	5 15	1 2	3 3	3 1		2 4			15	-1	15	15
80-84	4	3	5	3	4	6				40	-7	28	280
85-89	3 12	3 9	4 8	5 5	2 4	4 10	2 6	1 3	4 4	35	+1	35	35
90-94			2 4	3 2	4 8	1 4	3 6	1 8		13	+2	26	52
95-100										-	-	-	-
f	14	13	13	16	26	21	14	5	2	N=124	61	322	
d	-7	-3	-2	-1	0	+1	+2	+3	+4				
fd	56	39	26	16	-138	21	28	15	8	72			
fd²	224	117	52	16		21	56	45	32	563			

$$\sigma = \frac{1 - 0,350^2}{\sqrt{124}} = \frac{1 - 0,0625}{11,13} = \frac{0,9375}{11,13} = 0,084$$

$$\Sigma(x) = 181$$

$$c = \frac{-18}{124} \times 5 = -0,145 \times 5 = -0,725$$

$$M = 82,5 - 0,725 = 81,775$$

$$\sigma = 5 \sqrt{\frac{322}{124} - 0,145^2} = 5 \times 1,604 = 8,020$$

$$O.V. = \frac{8,020}{81,775} = 9,8$$

Variável x

$$c = \frac{-65}{124} \times 5 = -0,524 \times 5 = -2,620$$

$$M = 72,5 - 2,620 = 69,880$$

$$\sigma = 5 \sqrt{\frac{563}{124} - 0,524^2} = 5 \times 2,065 = 10,325$$

$$O.V. = \frac{10,325}{69,880} = 14,7$$

Coeficiente de correlação

$$r = \frac{\frac{181}{124} - (0,145 \times 0,524)}{8,020 \times 10,325} \times 25 =$$

$$= \frac{1,459 - 0,075980}{82,806500} \times 25 =$$

$$= \frac{1,383020}{82,806500} \times 25 =$$

$$= 0,010 \times 25 = 0,250$$

Nota = variável x

Mental level

Variável y

$$c = \frac{-203}{756} \times 2 = -0,268 \times 2 = -0,536$$

$$M = 26 - 0,536 = 25,464$$

$$\sigma = 20 \sqrt{\frac{2603}{756} - 0,268^2} = 2 \times 1,836 = 3,672$$

$$C.V. = \frac{3,672}{25,464} \times 100 = 14,4$$

Variável x

$$c = \frac{-228}{756} \times 5 = -0,301 \times 5 = -1,505$$

$$M = 67,5 - 1,505 = 65,995$$

$$\sigma = 5 \sqrt{\frac{9432}{756} - 0,301^2} = 5 \times 3,519 = 17,595$$

$$C.V. = \frac{17,595}{65,995} \times 100 = 26,6$$

Coeficiente de correlação

$$r = \frac{\frac{-800}{756} - (-0,268 \times -0,301)}{3,672 \times 17,595} \times 10 =$$

$$= \frac{(-1,058 - 0,080668)}{64,608840} \times 10 =$$

$$= \frac{-1,138668}{64,608840} \times 10 =$$

$$= -0,018 \times 10 = -0,180$$

$$\sigma_r = \frac{1 - 0,180^2}{\sqrt{756}} =$$

$$= \frac{1 - 0,032400}{27,49} =$$

$$= \frac{0,967600}{27,49} = \pm 0,035$$

	0-4	5-9	10-14	15-19	20-24	25-29	30-34	35-39	40-44	45-49	50-54	55-59	60-64	65-69	70-74	75-79	80-84	85-89	90-94	f	d	fd	fd²
19-20								¹ 18 ₁₈			² 18 ₉	⁴ 24 ₆	⁵ 15 ₃		⁹ 27 ₃	⁵ 30 ₆	⁷ 42 ₇	⁵ 60 ₁₂	¹ 45 ₁₅	45	-3	-135	405
21-22				¹ 20 ₂₀	¹ 18 ₁₈	² 32 ₁₆	² 28 ₁₄	⁴ 48 ₁₂	³ 30 ₁₀	⁴ 48 ₈	⁴ 48 ₆	⁹ 36 ₄	¹⁸ 36 ₂	¹⁰	²⁶ 52 ₂	²⁵ 100 ₄	¹⁷ 118 ₆	⁴ 128 ₈	⁴ 40 ₁₀	164	-2	-328	656
23-24		² 24 ₁₂	¹ 11 ₁₁		³ 18 ₉	³ 16 ₈	⁴ 28 ₇	³ 18 ₆	⁵ 25 ₅	⁵ 20 ₄	¹² 36 ₃	²¹ 42 ₂	²¹ 21 ₁	²⁰	³⁰ 30 ₁	¹⁵ 30 ₂	²⁴ 72 ₃	¹⁷ 68 ₄	⁴ 20 ₅	190	-1	-190	190
25-26	¹	¹		²	²	⁴	⁵	⁶	⁶	⁶	⁴	¹⁴	¹⁵	¹⁵	⁸	¹⁹	¹⁵	⁶	³	135	-6	-63	
27-28		² 22 ₁₁	³ 30 ₁₀	¹ 9 ₉	² 16 ₈		⁴ 24 ₆	³ 15 ₅	⁵ 20 ₄	⁶ 15 ₃	⁷ 44 ₂	¹³ 13 ₁	⁷	¹¹ 11 ₁	¹² 34 ₂	⁹ 27 ₃	⁹ 36 ₄	⁵ 25 ₅	103	+1	+103	103	
29-30				¹ 18 ₁₈	¹ 16 ₁₆	³ 42 ₁₄	³ 36 ₁₂	⁵ 50 ₁₀		⁴ 24 ₄	² 8 ₄	⁷ 44 ₂	⁴	⁷ 14 ₂	⁷ 28 ₄	⁹ 54 ₆	⁸ 64 ₈			64	+2	+128	256
31-32					² 48 ₂₄	¹ 21 ₂₁		¹ 15 ₁₅	¹ 12 ₁₂	¹ 9 ₉	⁴ 24 ₆	⁴ 12 ₃	²	⁵ 15 ₃	⁶ 36 ₆	⁶ 54 ₉				33	+3	+99	297
33-34		¹ 48 ₄₈			¹ 36 ₃₆				¹ 20 ₂₀					¹	¹ 4 ₄			¹ 20 ₂₀		6	+4	+24	96
35-36				¹ 48 ₄₈					¹ 25 ₂₅	¹ 20 ₂₀		² 20 ₁₀	¹ 5 ₅			X				6	+5	+30	150
37-38					² 96 ₄₈		¹ 36 ₃₆		¹ 24 ₂₄			¹ 6 ₆	¹		¹ 12 ₁₂					7	+6	+42	252
39-40								¹ 35 ₃₅		¹ 21 ₂₁										2	+7	+14	98
41-42																				-	-	-	-
43-44																				-	-	-	-
45-46											¹ 10 ₁₀									1	+10	+10	100
f	1	4	3	6	9	15	15	21	25	25	42	63	86	70	97	95	100	61	18	450	+303	+2603	
d	-13	-12	-11	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1		+1	+2	+3	+4	+5				
fd	-13	-48	-33	-60	-81	-120	-105	-136	-125	-100	-126	-126	-86	-109	+97	+190	+300	+244	+90	921			
fd²	169	576	363	600	729	960	735	756	625	400	378	372	86		97	380	900	976	450	9432			

$$\Sigma(-xy) = -800$$

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(Nível Mental)

Idade = variável x

	11-12	13-14	15-16	17-18	f	d	fd	fd ²
0-4						-	-	-
5-9			1 5		1	-5	-5	25
10-14	21					-	-	-
15-19	16				4	-3	-12	36
20-24	12	3	4	1	14	-2	-28	56
25-29	3		4	1	14	-1	-14	14
30-34	3							
35-39	1	3	3	4	9	+1	+9	9
40-44	1	6	12		10	+2	20	40
45-49	21	6			10	+3	30	90
50-54		4			1	+4	4	16
55-59	21	26	4		63			386
60-64	1				1			
65-69	1				1			
70-74	21	1			22			
75-79	21				22			
80-84	21				22			

$$\Sigma(x) = 6$$

Variável y

$$c = \frac{4}{76} \times 5 = 0,052 \times 5 = 0,260$$

$$M = 32,5 + 0,260 = 32,760$$

$$\sigma = 5 \sqrt{\frac{286}{76} - 0,052^2} = 5 \times 1,939 = 9,695$$

$$C.V. = \frac{9,695}{32,760} \times 100 = 29,5$$

Variável x

$$c = \frac{13}{76} \times 2 = 0,171 \times 2 = 0,342$$

$$M = 14 + 0,342 = 14,342$$

$$\sigma = 2 \sqrt{\frac{63}{76} - 0,171^2} = 2 \times 0,893 = 1,786$$

$$C.V. = \frac{1,786}{14,342} \times 100 = 12,4$$

Coefficiente de correlação

$$r = \frac{6}{76} - \frac{(0,260 \times 0,342)}{9,695 \times 1,786} \times 10 =$$

$$= \frac{0,078 - 0,088920}{17,315270} \times 10 =$$

$$= \frac{-0,010920}{17,315270} \times 10 =$$

$$= -0,0006 \times 10 = -0,006$$

$$r_{\pi} = \frac{1 - 0,006^2}{\sqrt{76}} =$$

$$= \frac{1 - 0,000036}{8,71} =$$

$$= \frac{0,999964}{8,71} = \pm 0,114$$